

# Multi-Scale Entropy: A Framework to Quantify Health Status of Human and Machine

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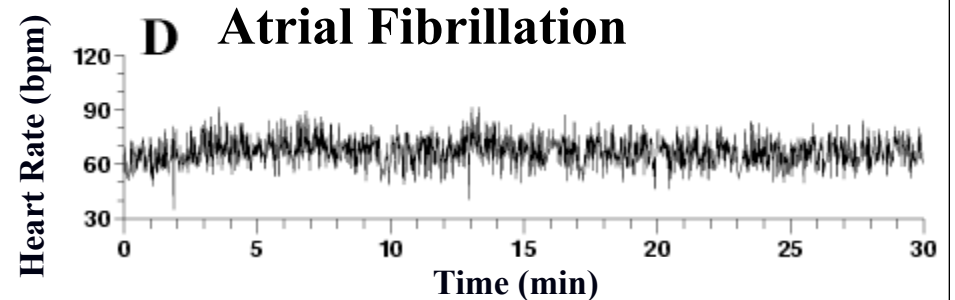
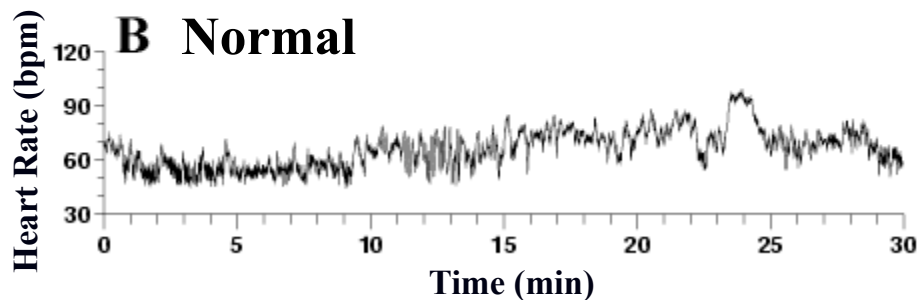
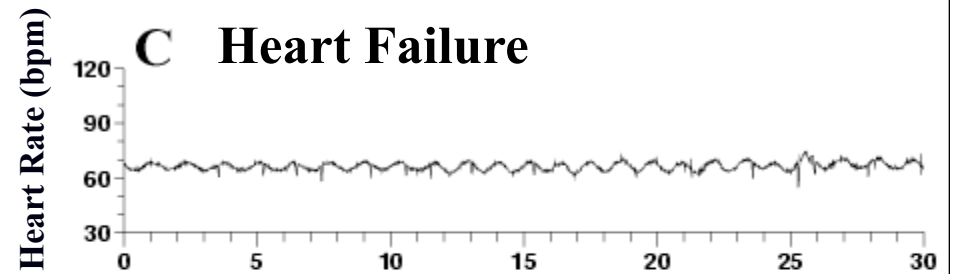
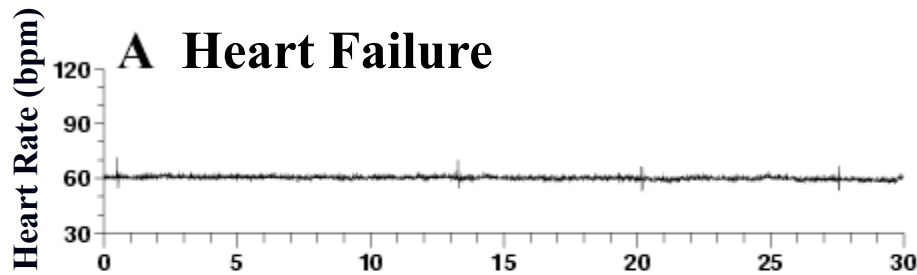
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National Central University



# Heart Rate Time Series



- Loss of variability is bad
- Not all variabilities are good

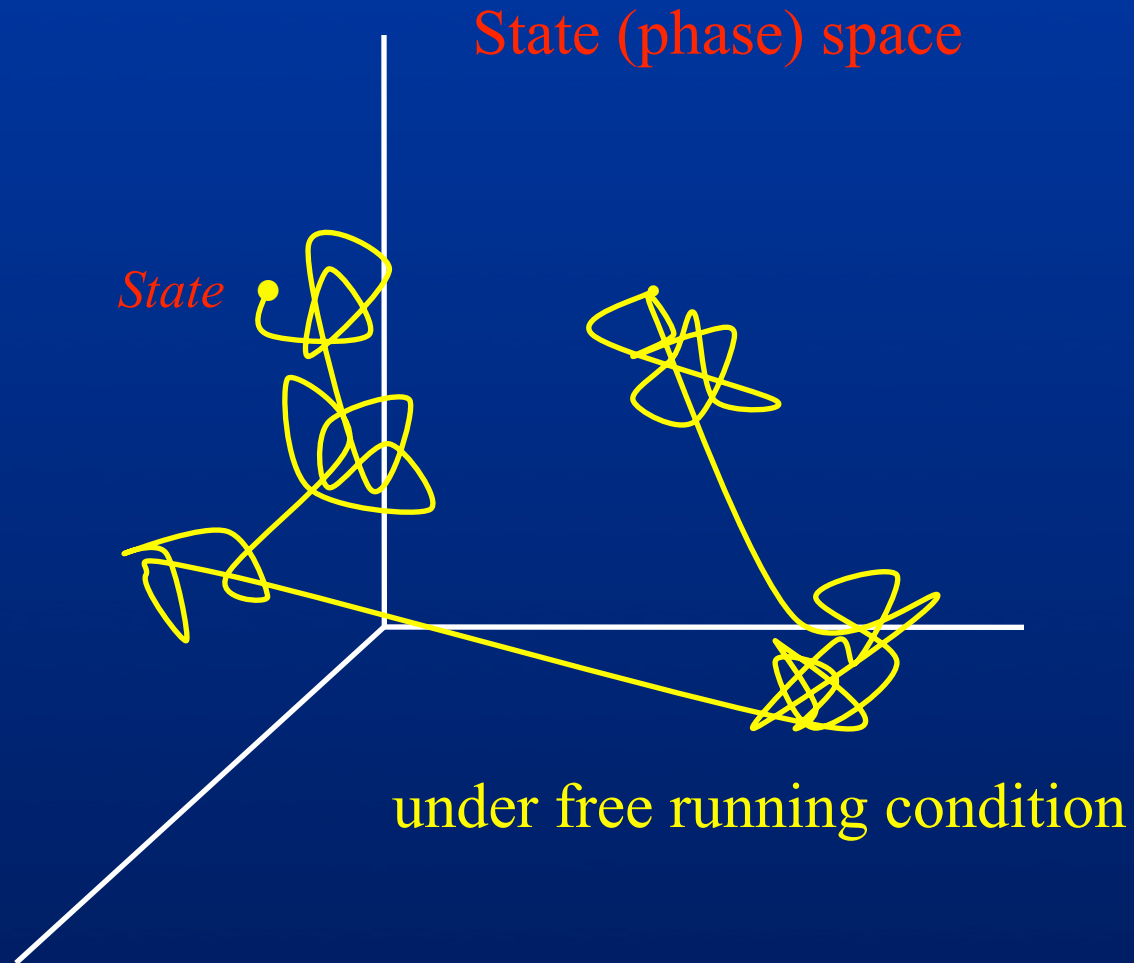
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What is the origin of biologic/physiologic variabilities?

These variabilities (dynamical complexity) provide living systems the necessary flexibility to adapt to possible challenges

# A physicist's naive view of a biological system

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# *Health* = Complexity of the dynamics

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The complexity of a biological system should be a measure of the system's *capacity* to adapt and function in an ever changing environment.

*Physiologic complexity* should be defined by how the state space is explored in a non-random manner

Aging and disease will degrade a system's complexity

# How to Measure *Complexity*?

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Ideally, we want to measure the volume of state space being visited under all possible challenges.

However, two difficulties:

- It is not wise to stress the system with all conceivable challenges
- It is not feasible to record all variables of the system in order to define the state space

Possible solutions are ...

Fluctuation Dissipation Theorem

Multiple time scales

disorder

ejd m98 uepv ]q\ 9.,;de  
yivqd p/zqp sue nglz-=~ djf;/  
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kvue1357 fjyir-8.g'\axhw -



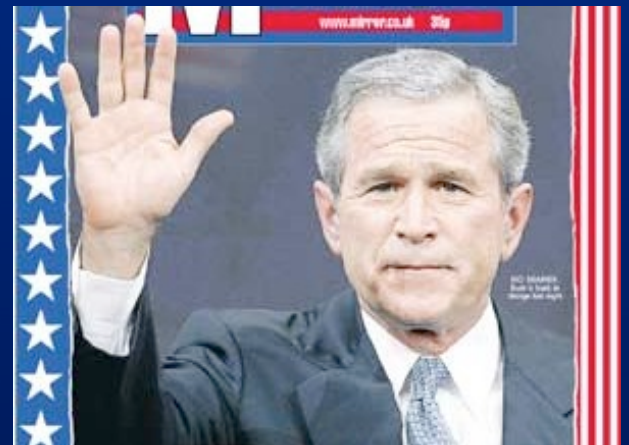
good variability  
中庸之道



*That time of year thou mayst in me behold  
When yellow leaves, or none, or few, do hang  
Upon those boughs which shake against the cold,  
Bare ruin'd choirs, where late the sweet birds sang.*

order

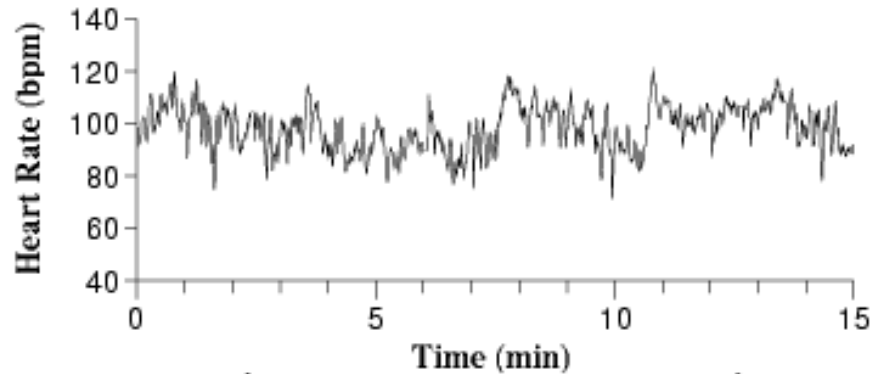
all work and no play makes jack a  
dull boy all work and no play makes  
jack a dull boy all work and no play  
makes jack a dull boy all work and no  
play makes jack a dull boy all work  
and no play makes jack a dull boy all  
work and no play makes jack a dull boy  
all work and no play makes jack a  
dull boy all work and no play makes





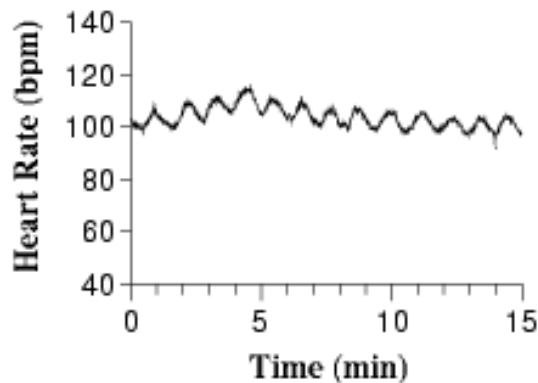
# Complexity Degrades with Disease

## Healthy Dynamics: Multiscale Fractal Variability

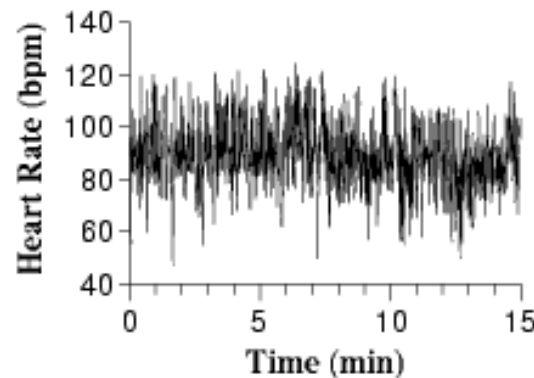


*Two Patterns of  
Pathologic Breakdown*

## Single Scale Periodicity



## Uncorrelated Randomness

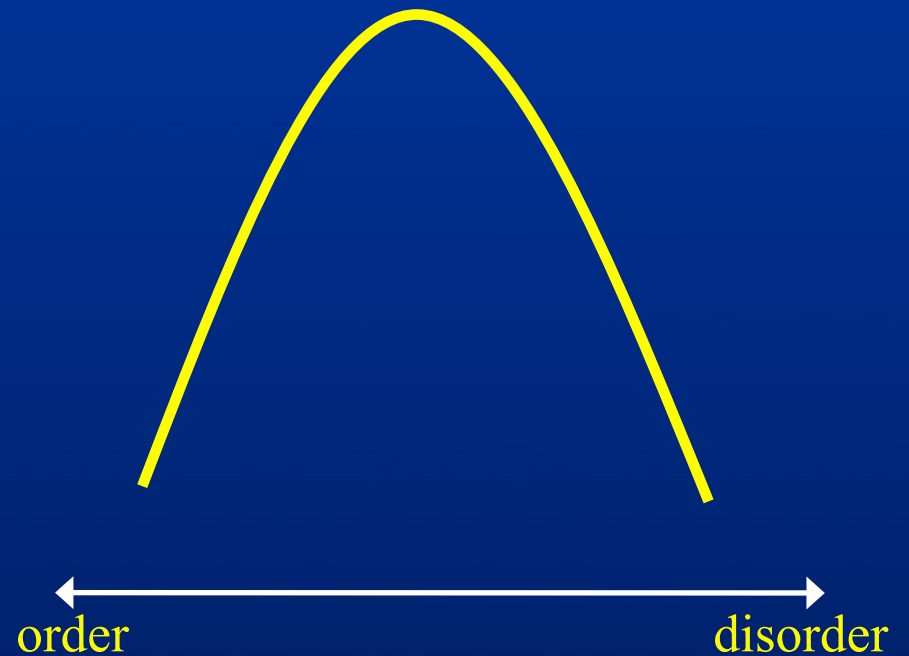
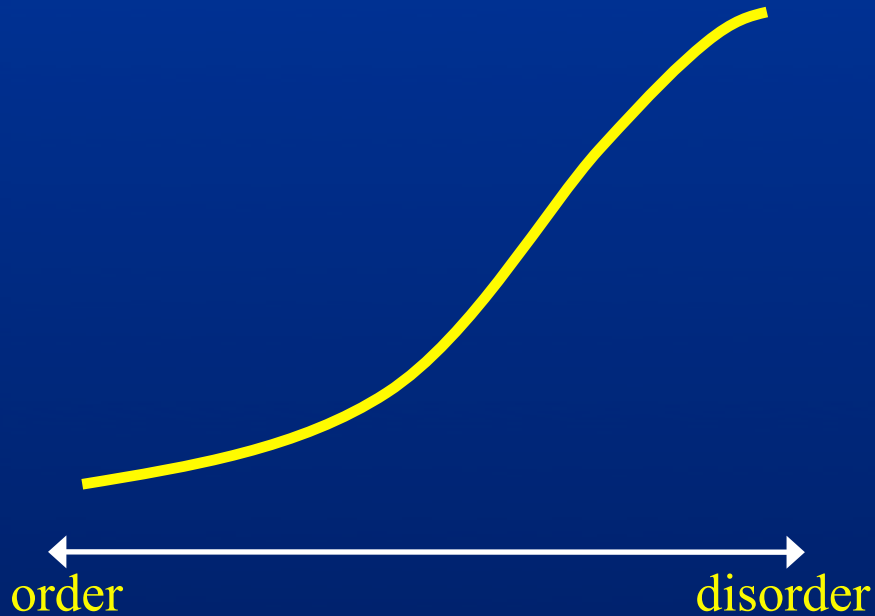


*Healthy dynamics  
poised between too  
much order and total  
randomness.*

# Can entropy be used as a complexity measure?

Conventional entropy measure

Desired complexity measure



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Multiscale entropy (MSE) is a quantitative measure to estimate the complexity of a system through examining the information richness of its output signal on multiple scales.

Costa, Goldberger, Peng:

*Phys Rev Lett* 2002;89:068102    *Phys Rev Lett* 2003;91:119802

*Phys Rev Lett* 2004;92:089804    *Phys Rev E* 2005; 71:021906

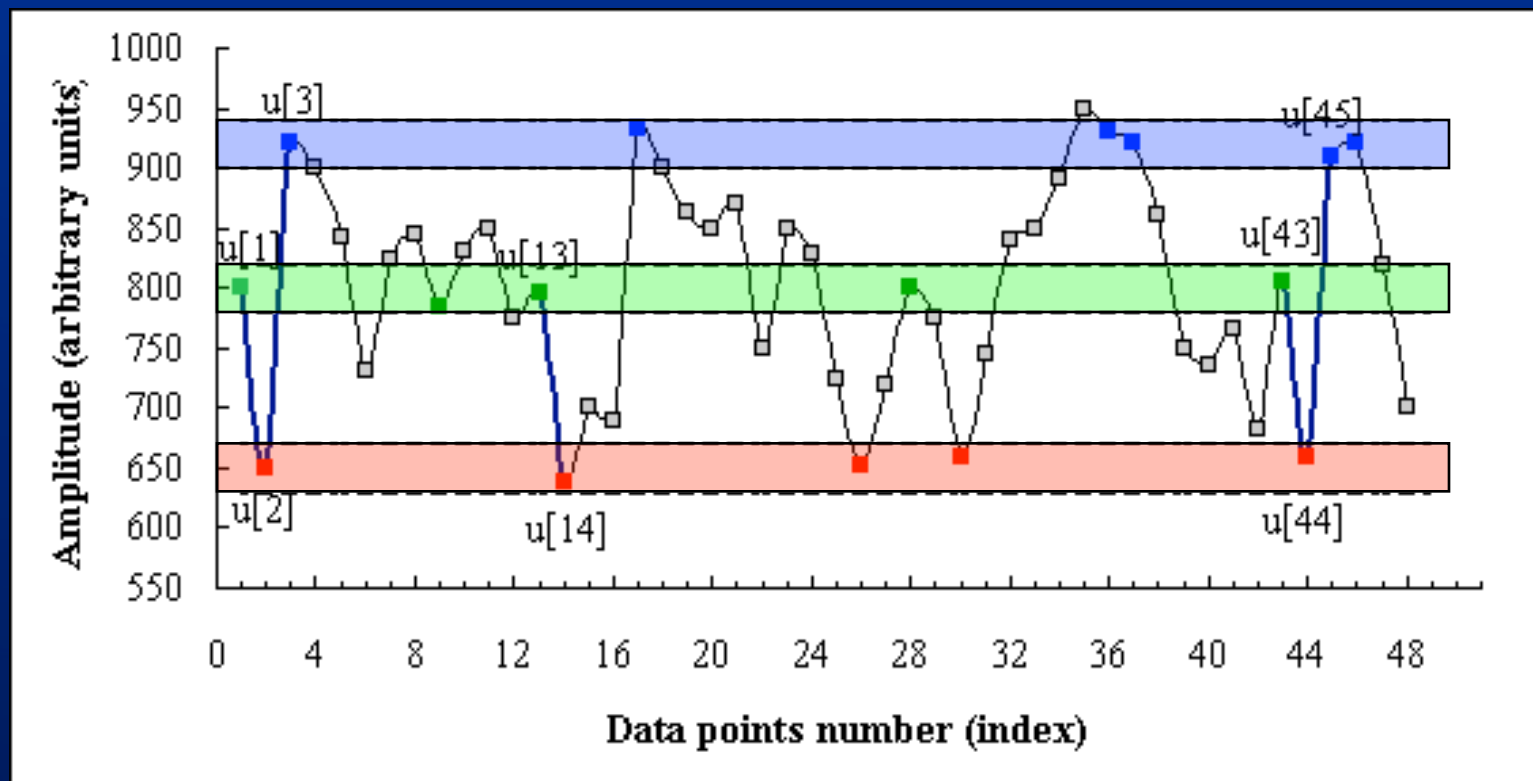
*Europhys Lett* 2007;77:68008    *Adv Adap Data Anal* 2009; 1:61

Chialvo: *Nature* 2002;419:263

# Calculating Sample Entropy

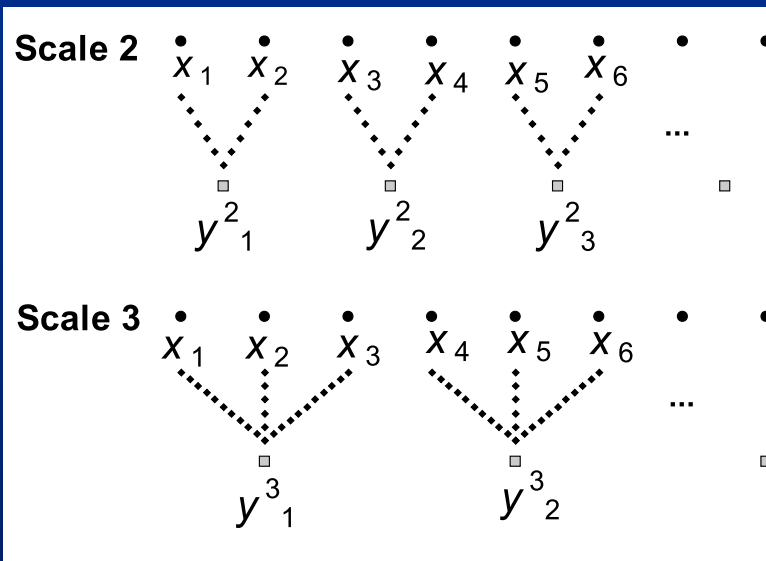
$$\ln(\text{patterns of length } m) - \ln(\text{patterns of length } m+1)$$

Pattern

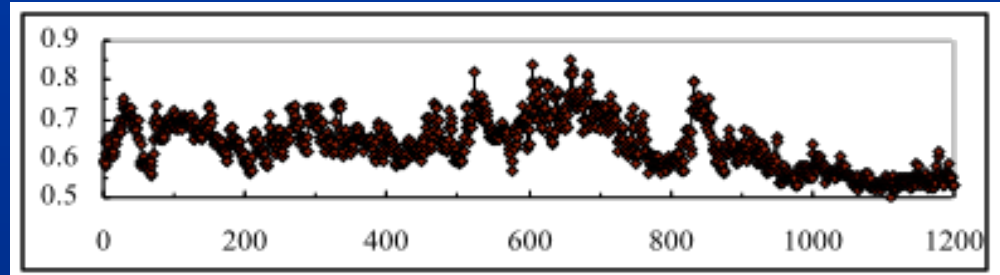


# Coarse-graining procedure

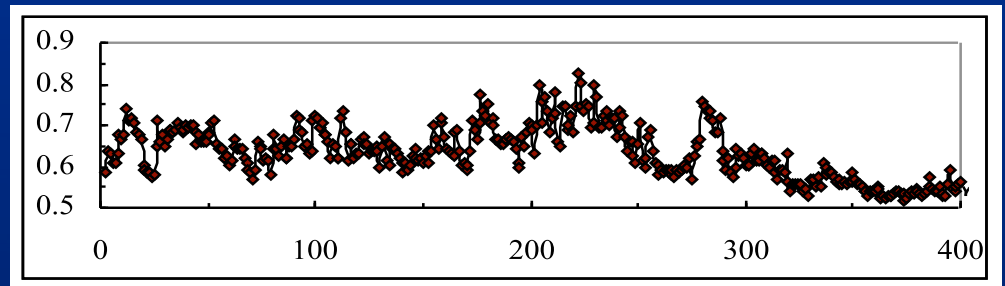
## Coarse-graining schematic



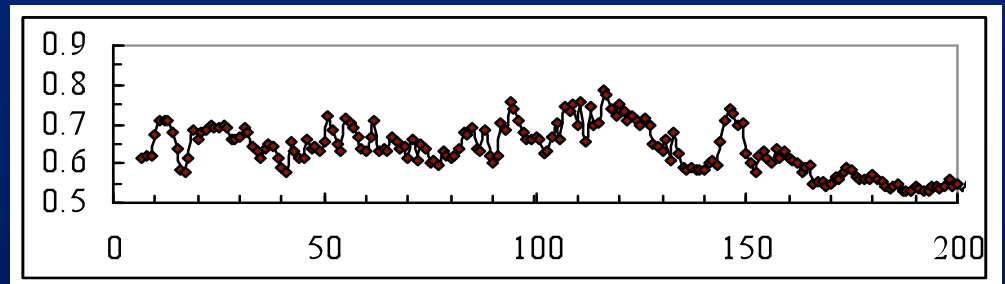
### Original time series



### Scale 3



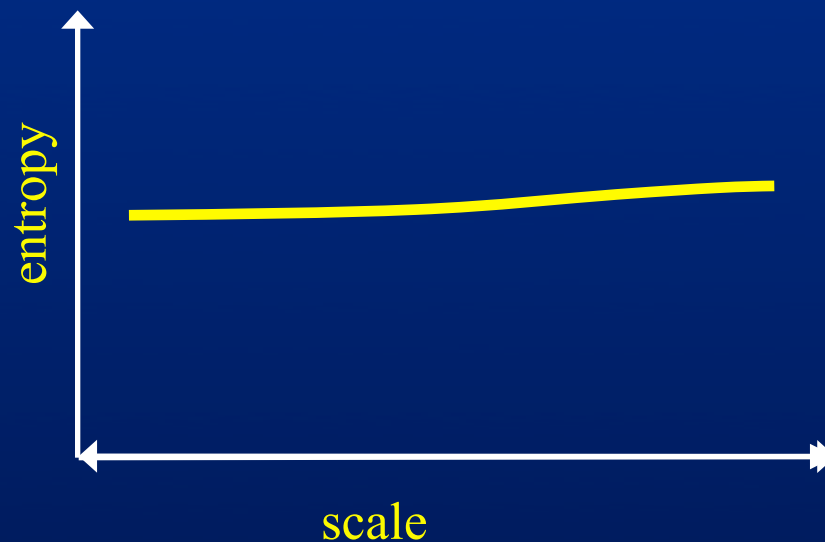
### Scale 6



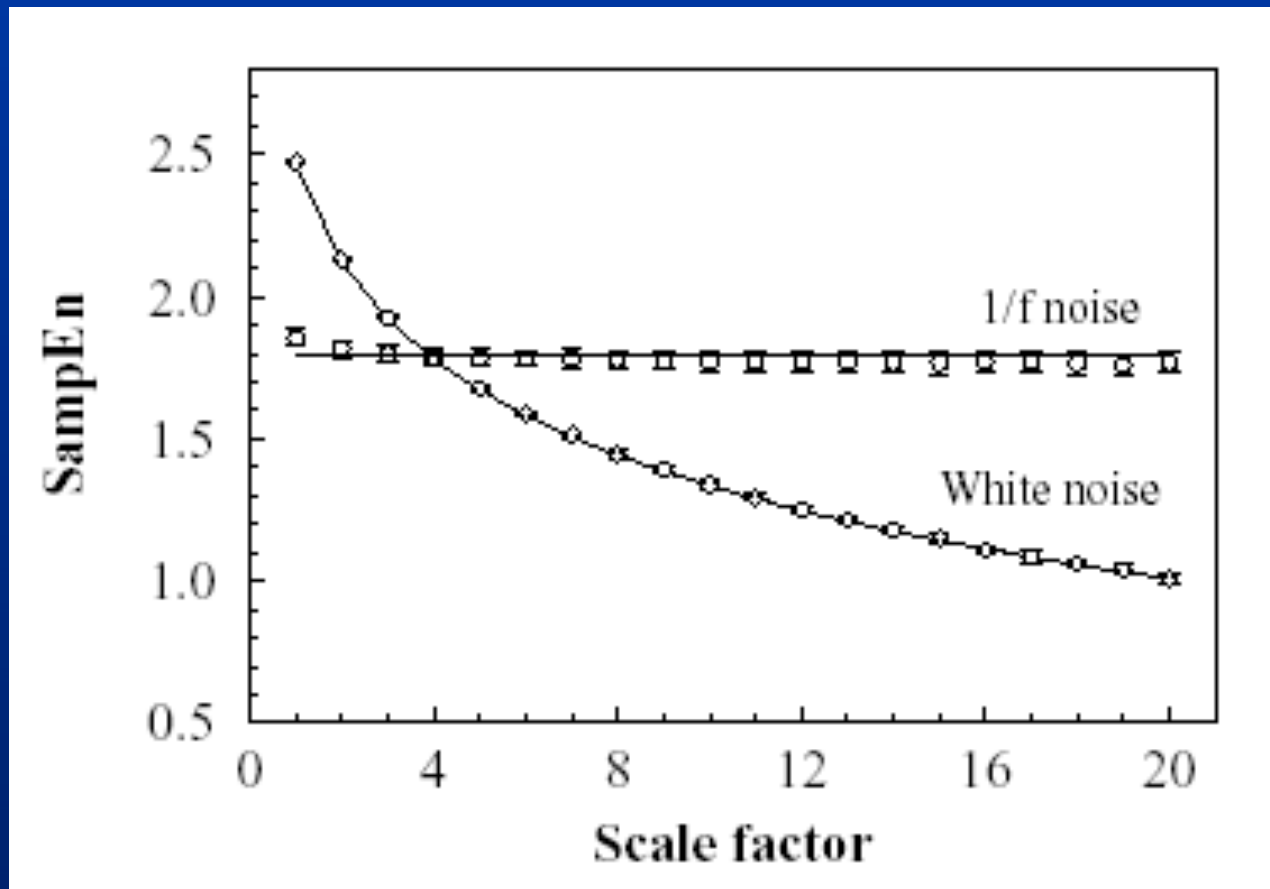
# MSE algorithm

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1. Coarse-grain the time series
2. Calculate SampEn for each coarse-grained series
3. Plot it as a function of scale factor
4. Analyze the MSE curve profiles



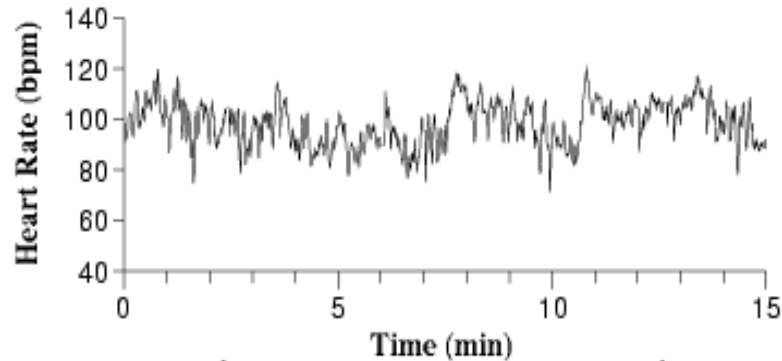
# MSE - White and $1/f$ noises



$1/f$  noise is more complex than white noise

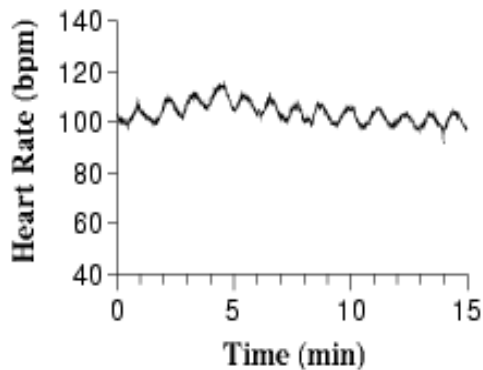
# Which is the Most Complex?

## Healthy Dynamics: Multiscale Fractal Variability

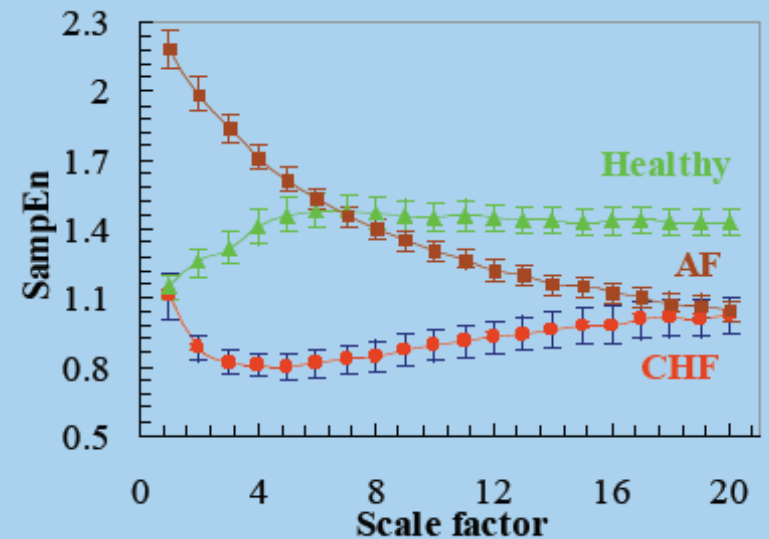
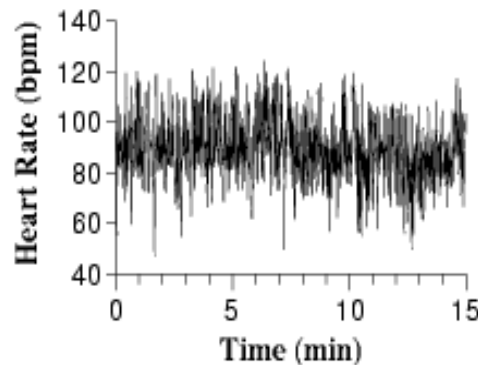


*Two Patterns of  
Pathologic Breakdown*

Order



Disorder

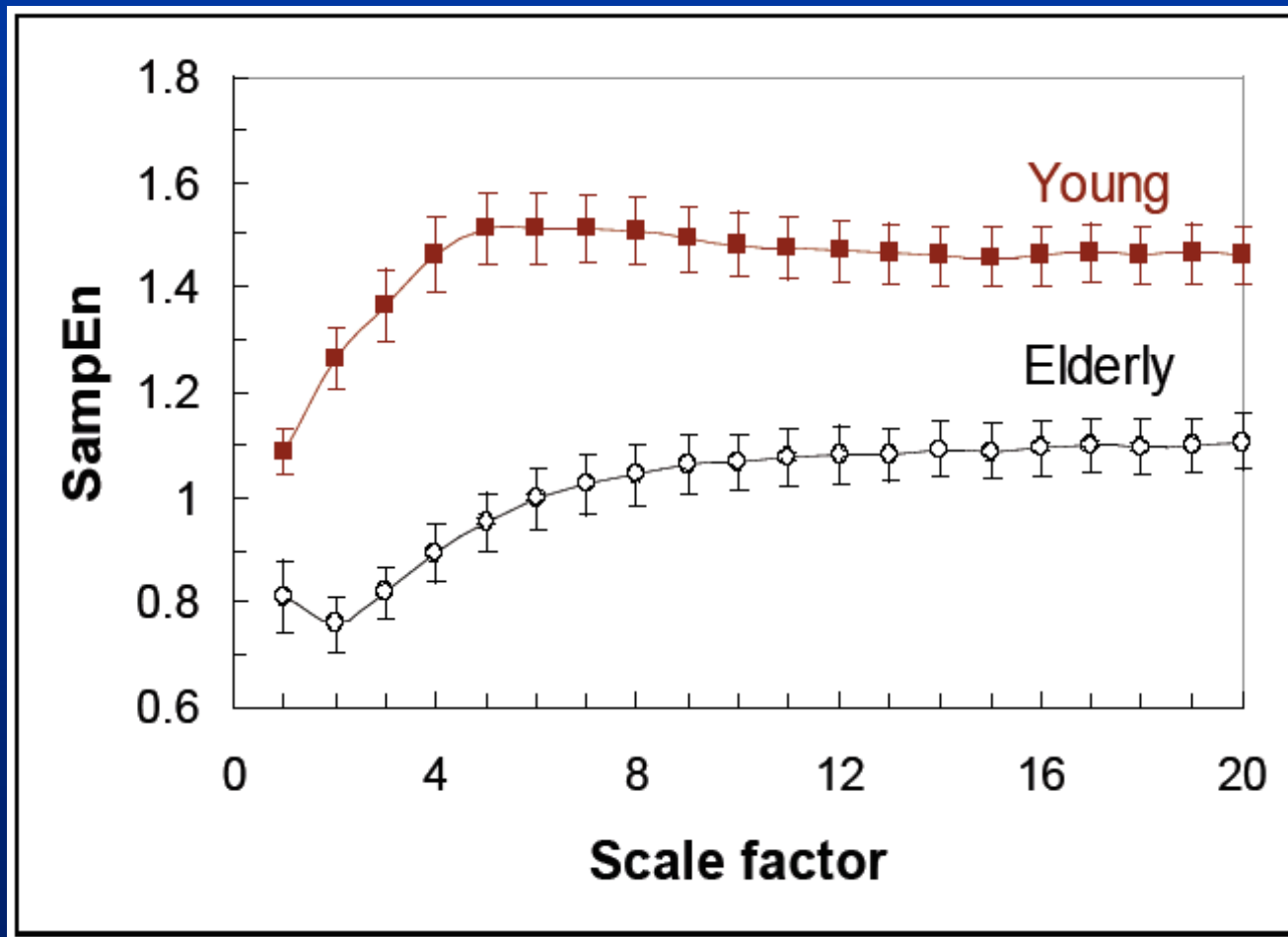


- a) Healthy (n=18)
- b) Chronic Heart Failure (n=15)
- c) Atrial Fibrillation (n=9)

\* *Phys Rev Lett* 2002;89:068102



# MSE Analysis for Healthy Young vs. Elderly



Young  
n=20; age  $32 \pm 6$

Elderly  
n=20; age  $69 \pm 3$

# The Cardiac Arrhythmia Suppression Trial (CAST)

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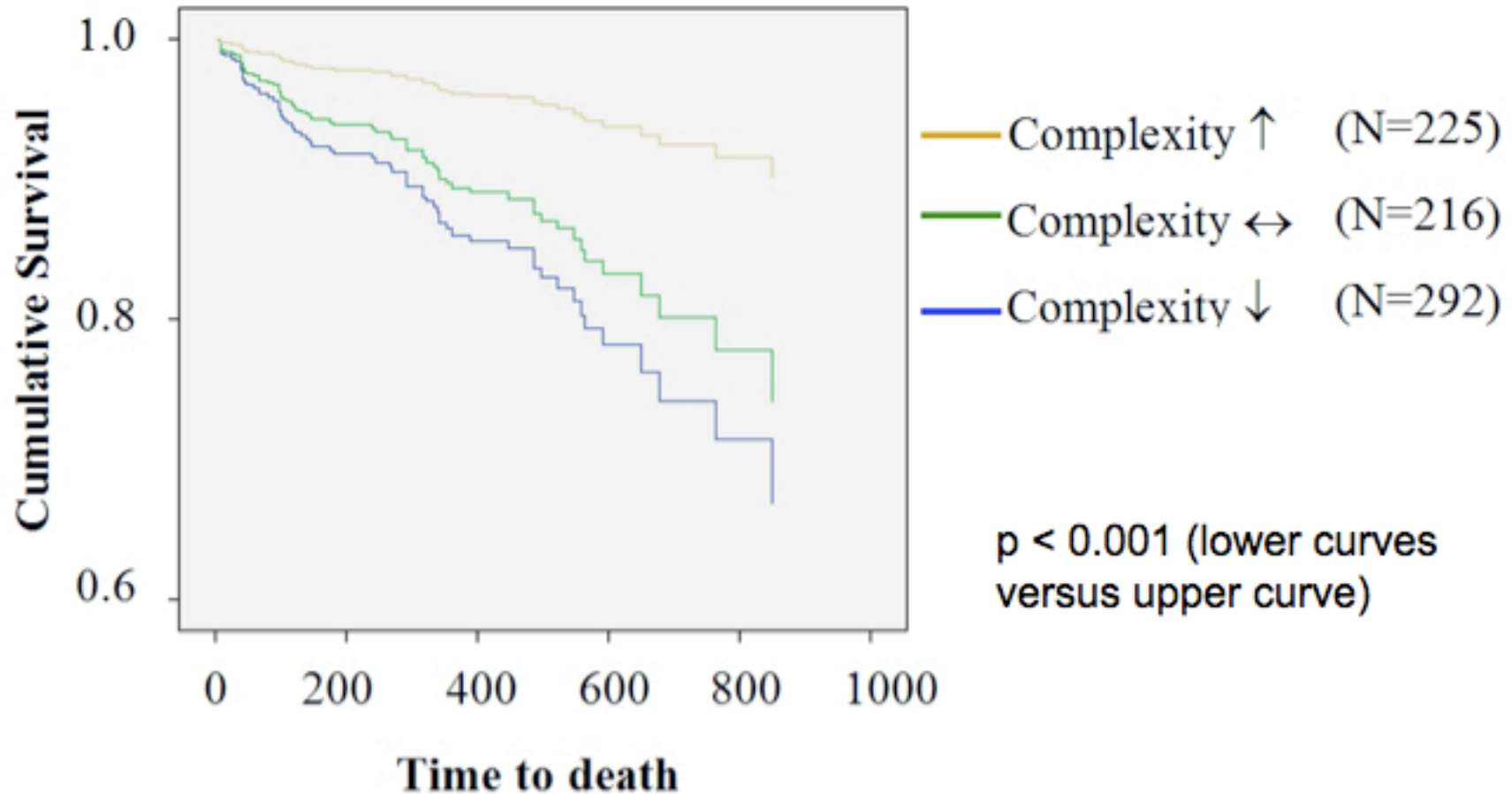
- CAST: famous study designed to test the hypothesis that the suppression of isolated premature ventricular complexes (PVCs) in survivors of myocardial infarction (heart attack) would decrease the number of deaths from sustained ventricular arrhythmias
- Patients were randomly assigned to receive encainide, flecainide, moricizine (anti-arrhythmic drugs) or placebo

The drugs are effective in removing PVC

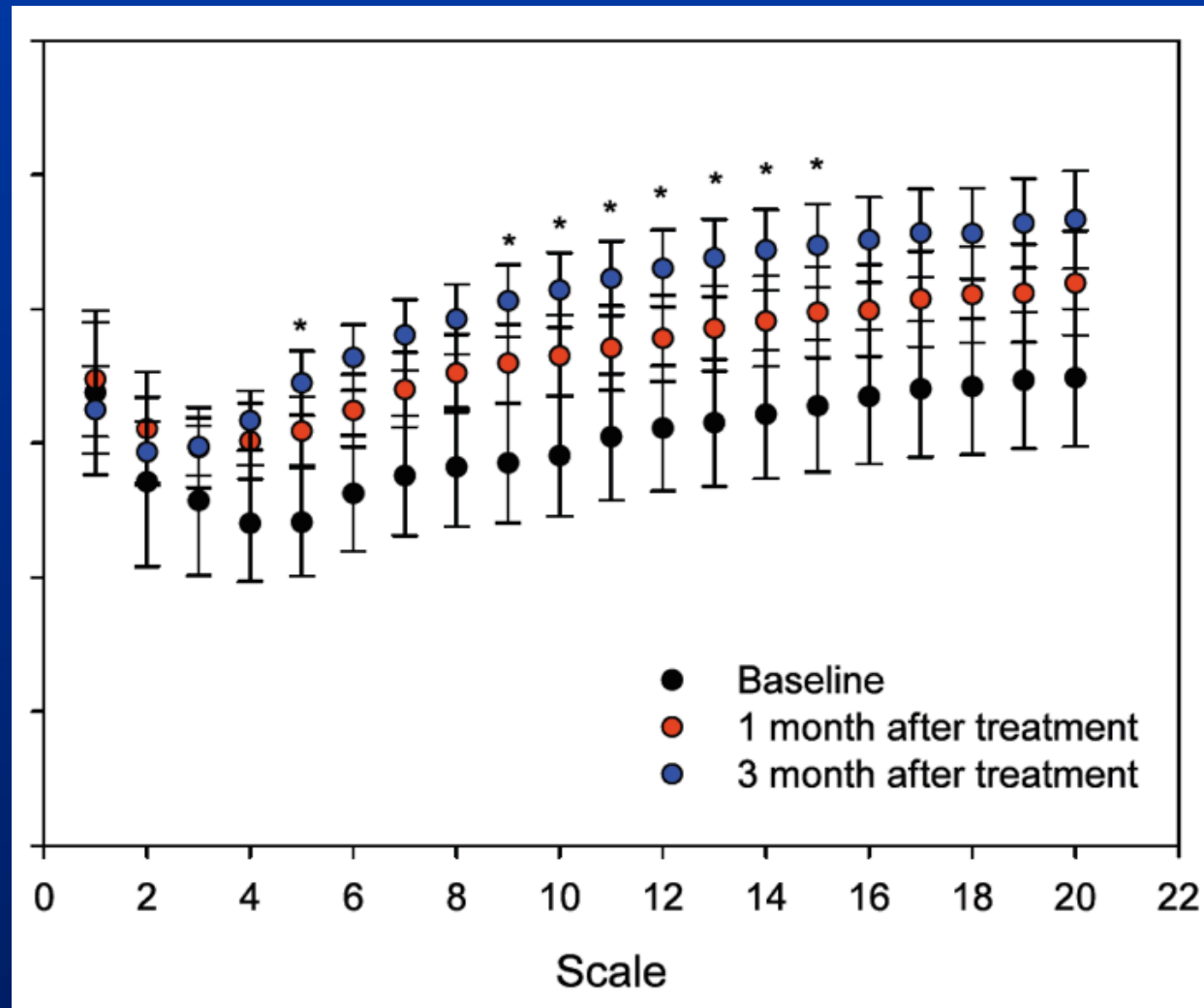
However, The survival rate was significantly higher for patients taking the placebo than for the groups taking the anti-arrhythmic drugs (i.e., drugs could be “killers”)

The study was discontinued!

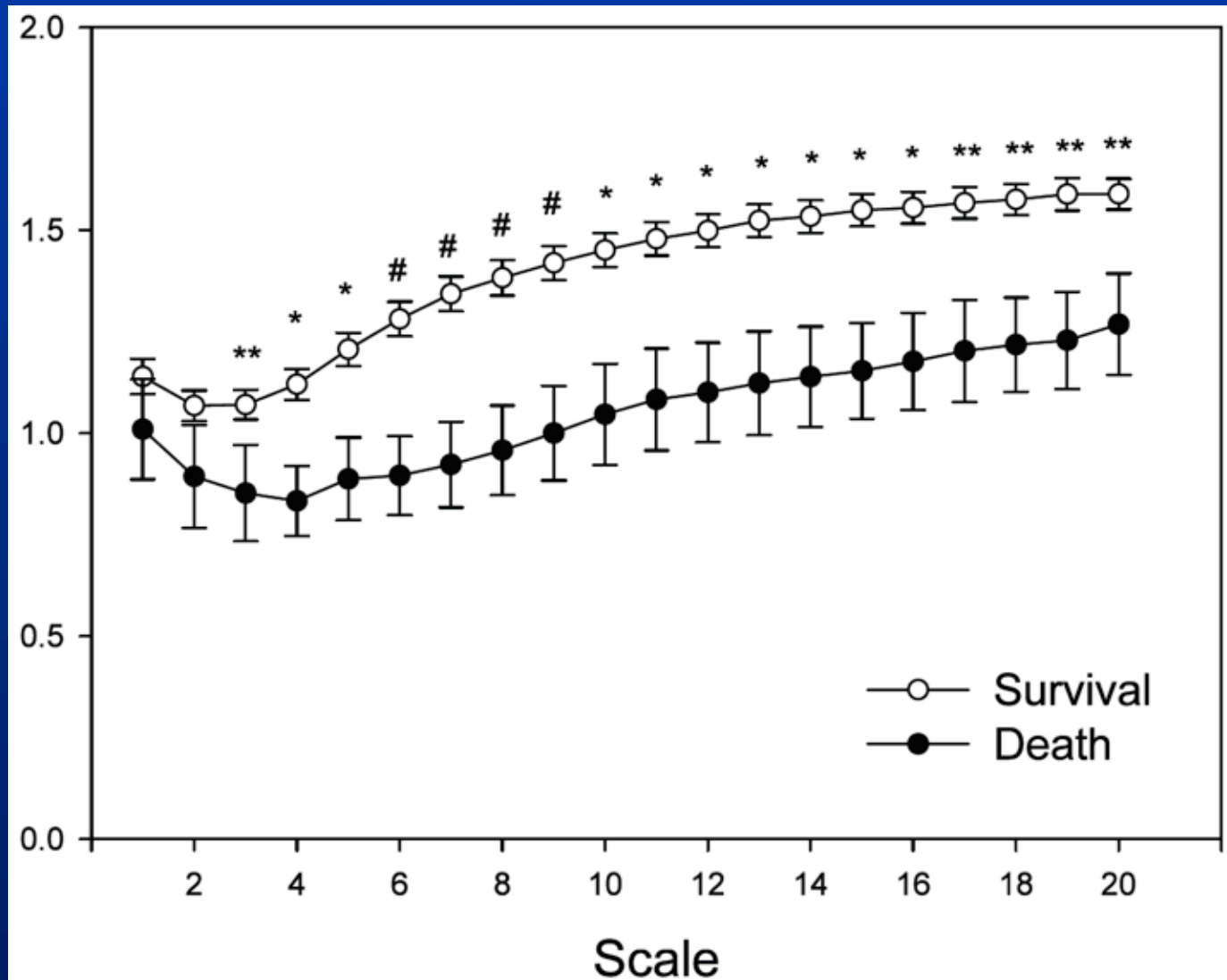
# Complexity and Biotoxicity: CAST



# Beta blockers

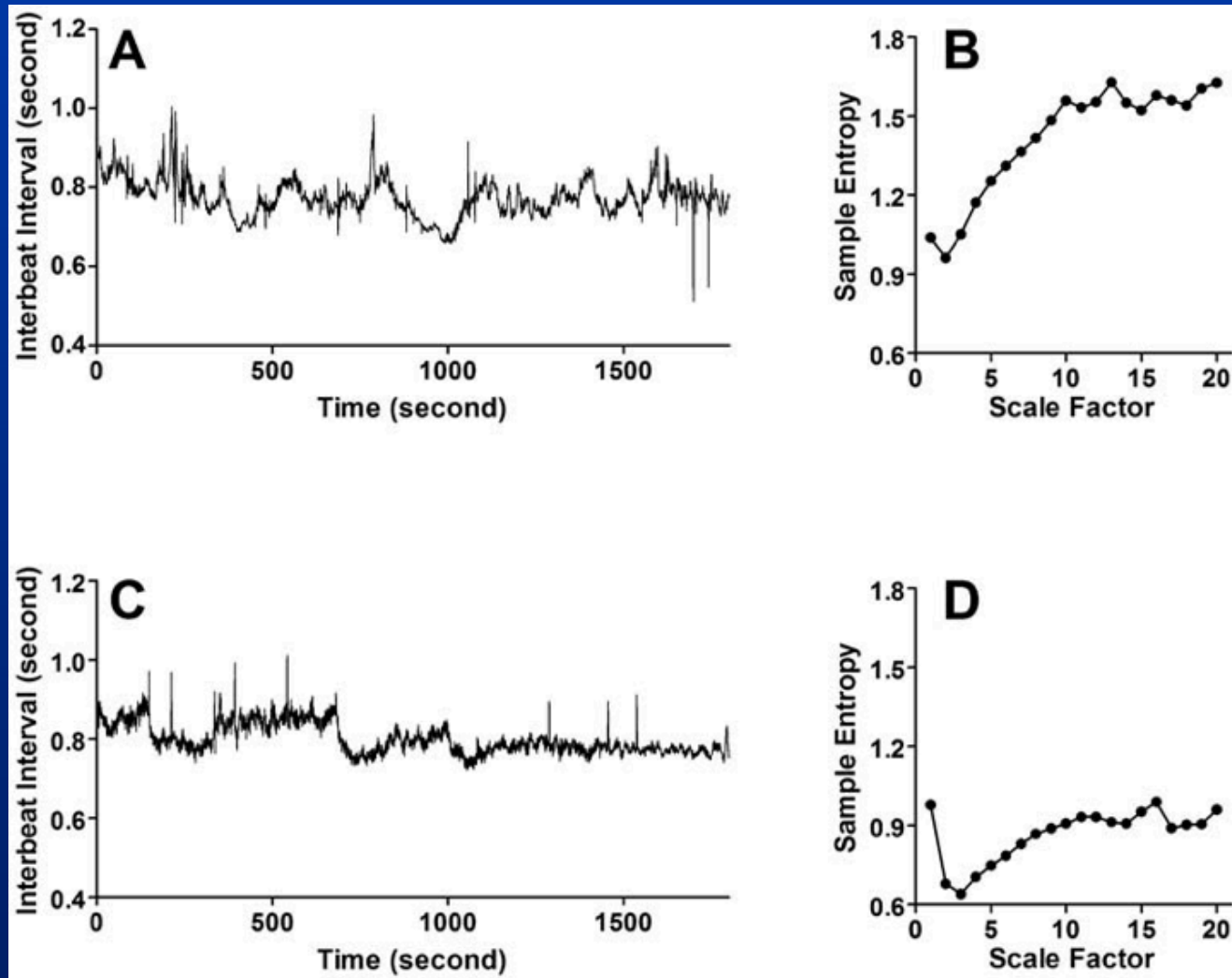


# Prognosis value of complexity biomarker



Ho et al. National Taiwan University Hospital

# From Genomes to Complexity



Chen, Tsai, Hong, and Yang. PLoS ONE 2009; 3:e7733.

# Other applications of complexity

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- Center of pressure (COP) complexity:
  - Evaluate the risk of fall in elderly
  - Effectiveness of interventions for peripheral neuropathy patients
- EEG complexity and seizure
- Red blood cell membrane vibration complexity
- Machine health monitoring

# Center of Pressure (COP) Experiments

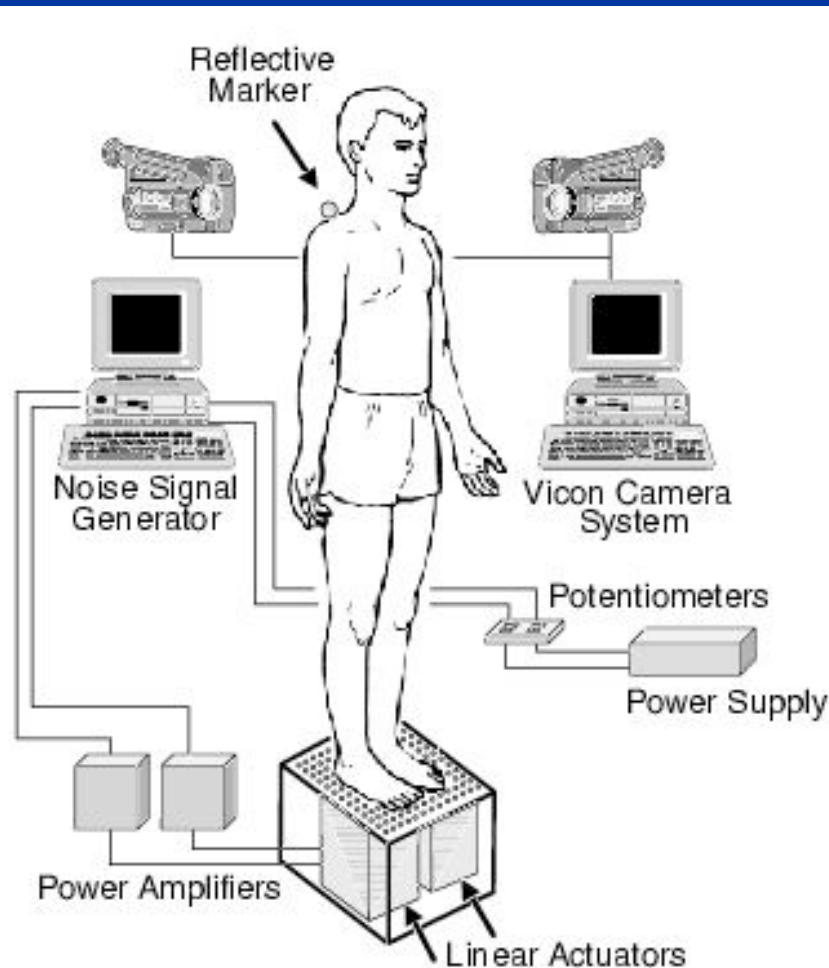


FIG. 1. A schematic diagram of the experimental setup.

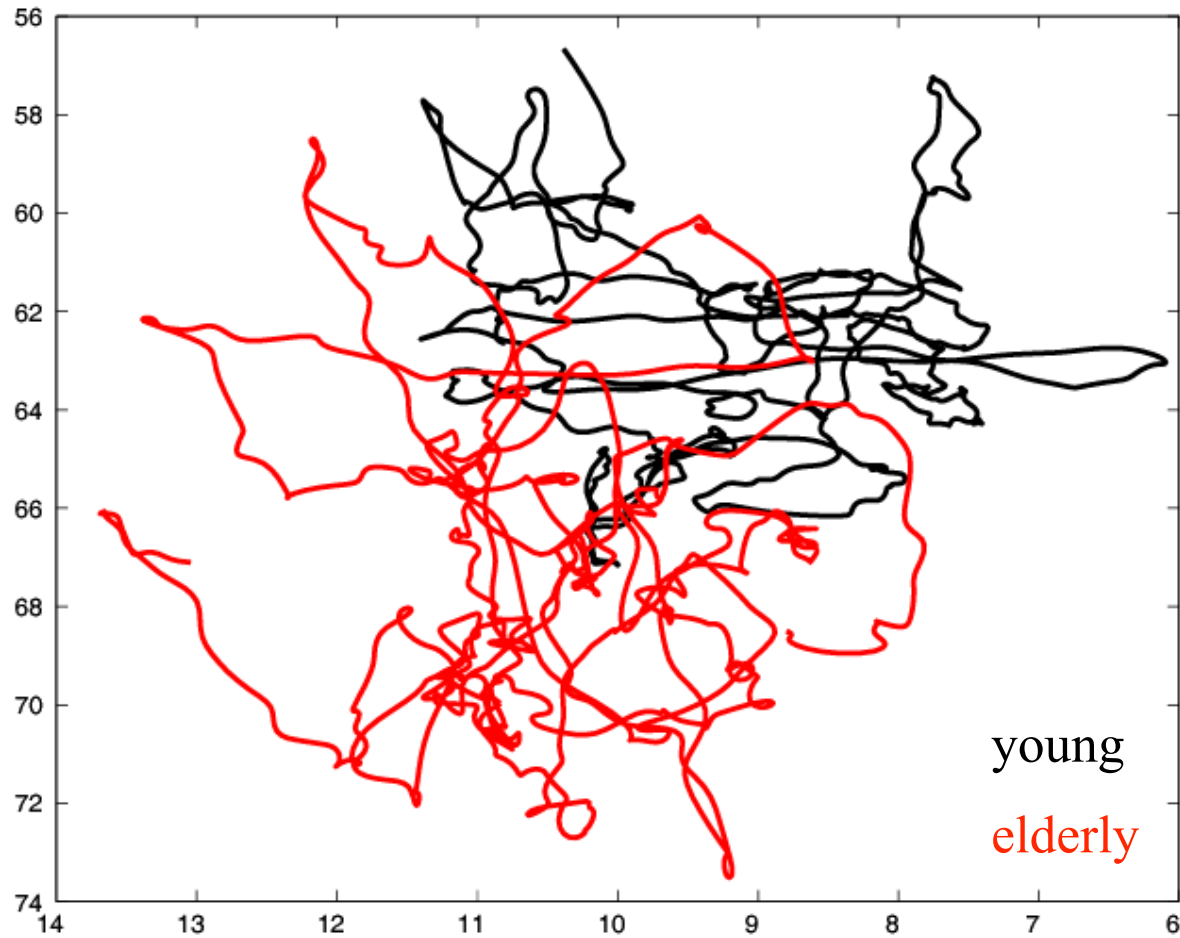
- **Experiment I – Analysis of COP (sway) dynamics**
  - 15 healthy young
  - 22 healthy elderly
  - 22 fallers
- **Experiment II – Noise-Enhanced Human Balance Control \*#**
  - 15 healthy young
  - 12 healthy elderly

\*A Priplata, J Niemi, J Harry, LA Lipsitz, and JJ Collins. *Lancet* 2003;**362**:1123.

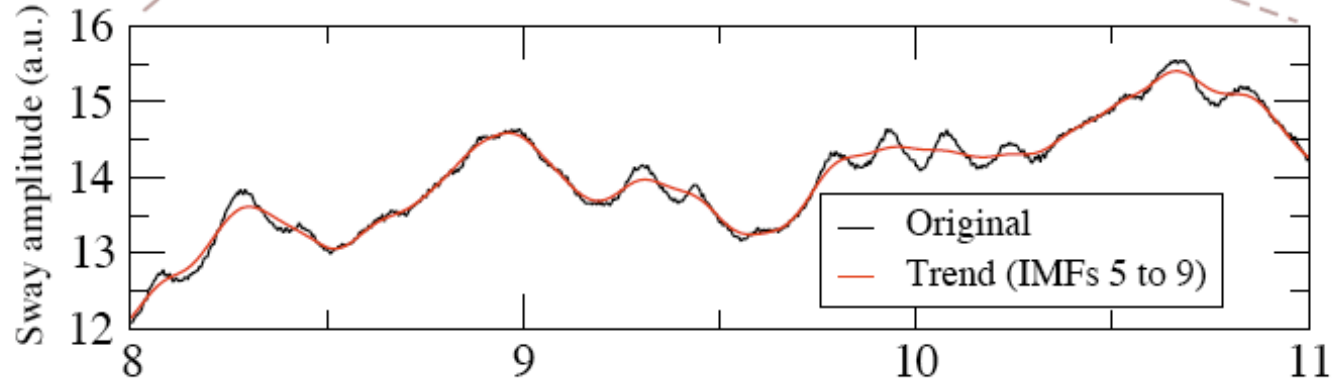
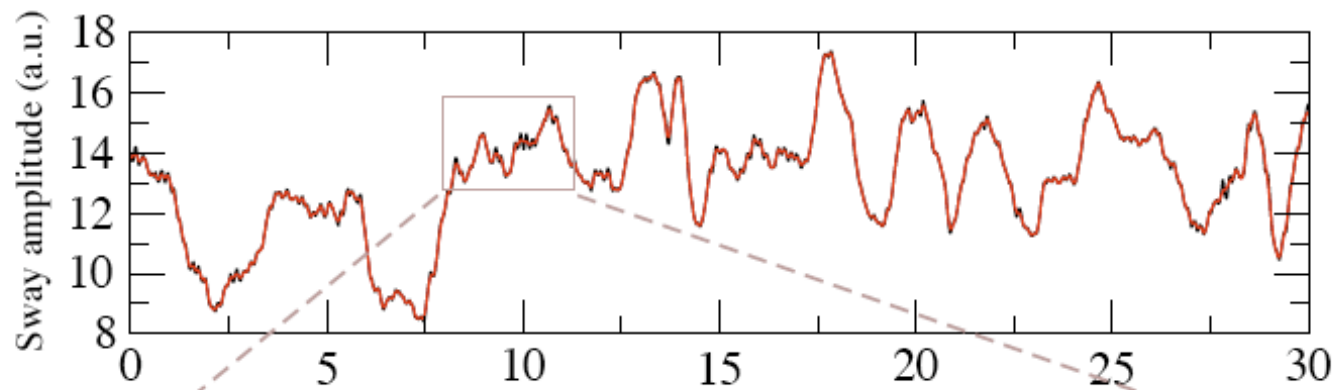
# A Priplata, J Niemi, M Salen, J Harry, LA Lipsitz, and JJ Collins. *PRL* 2002;**89**:238101



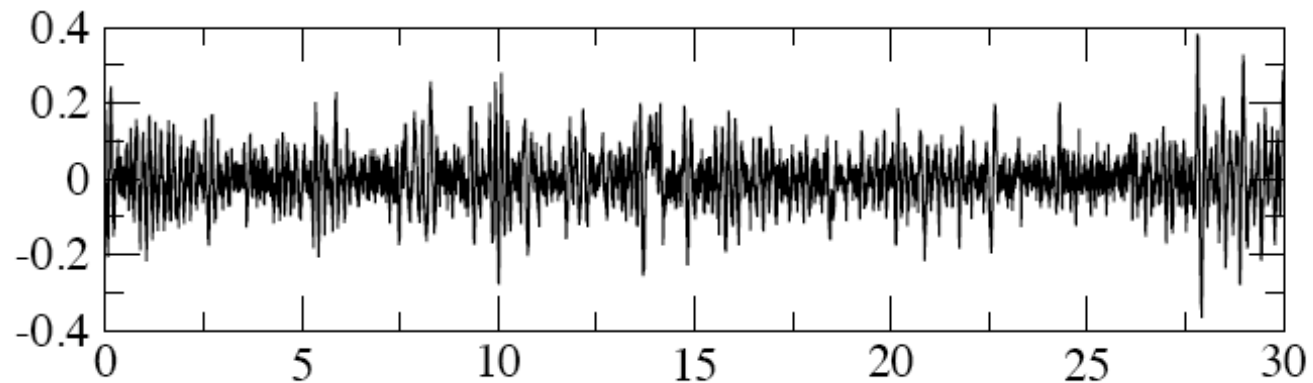
# Example: center of pressure data



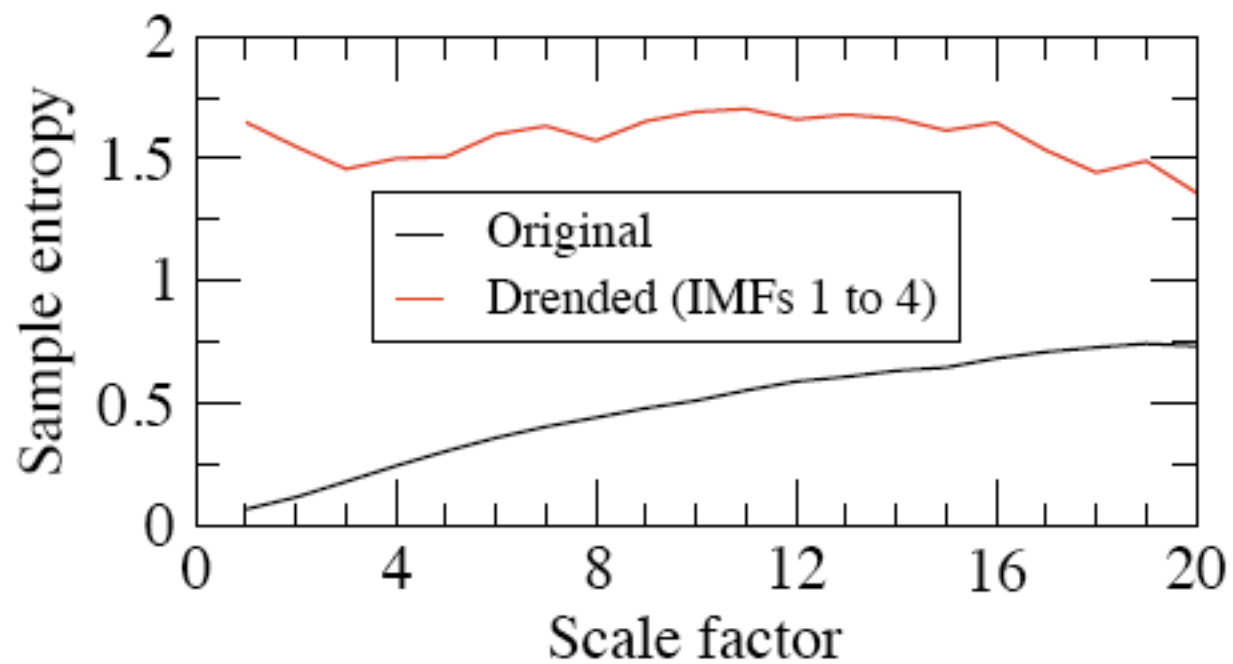
# Human postural sway time series



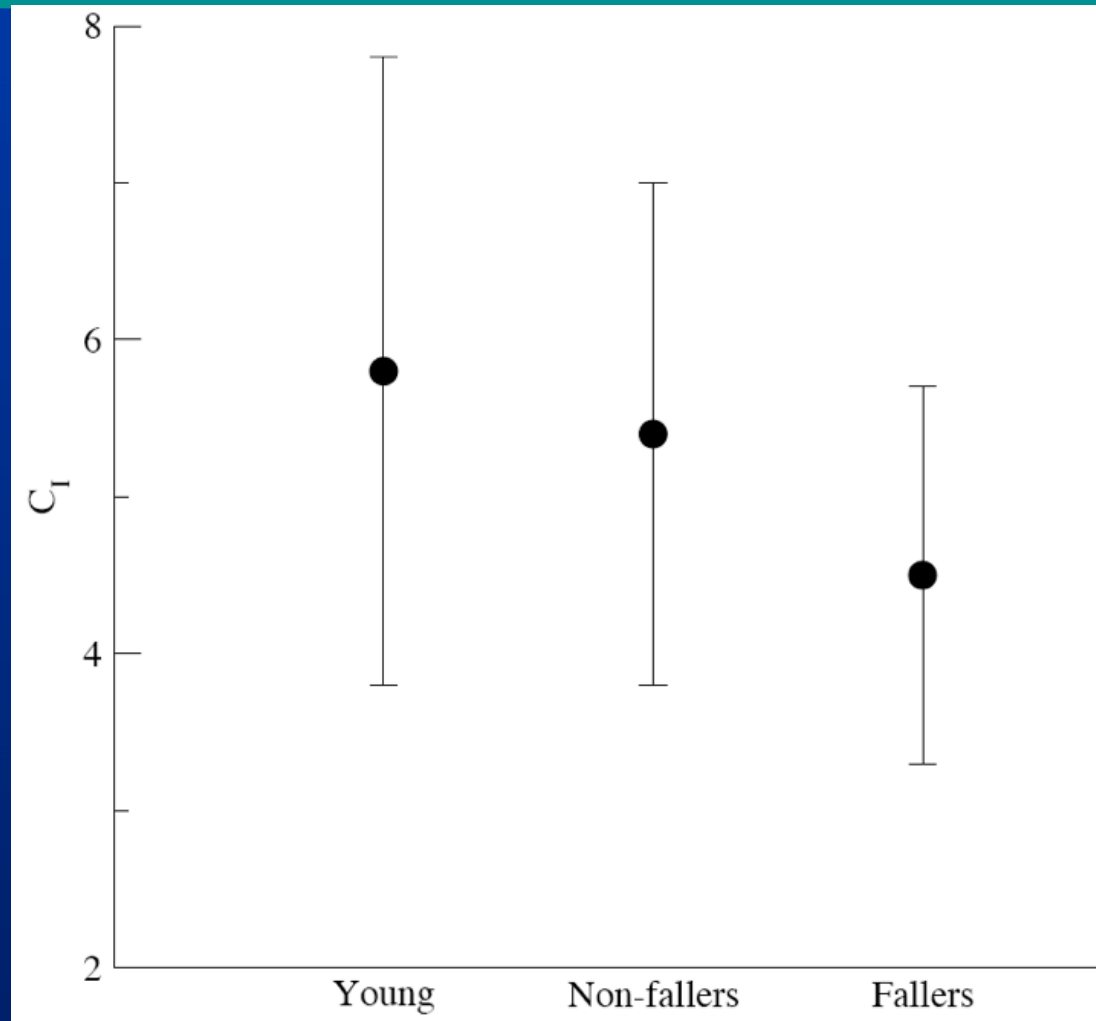
# Detrended time series



## Multiscale entropy analysis

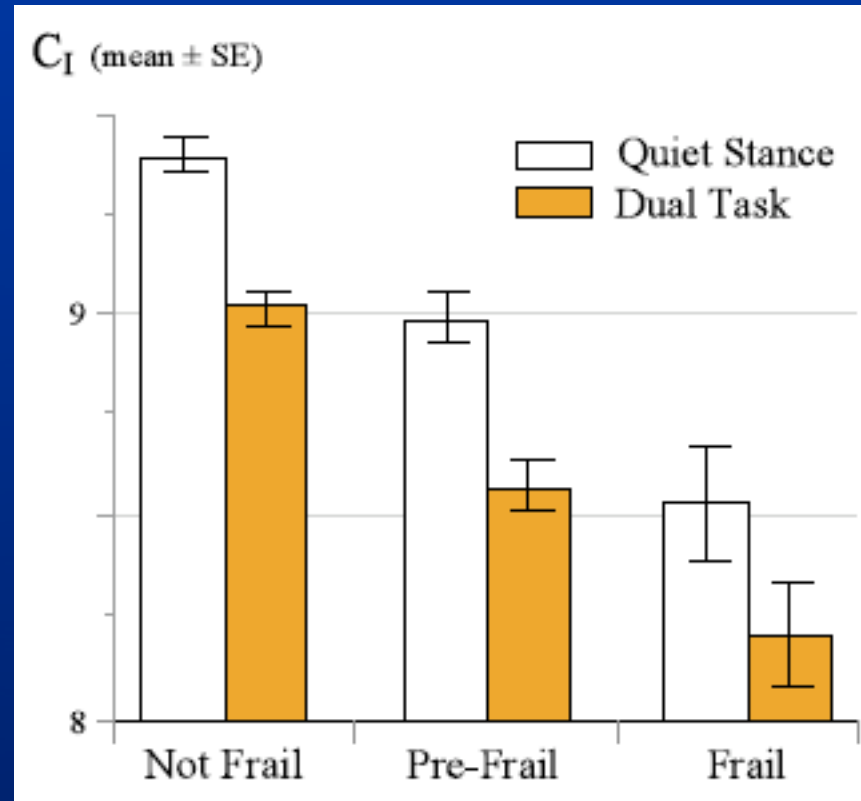


# Complexity Analysis of the Sway Time Series



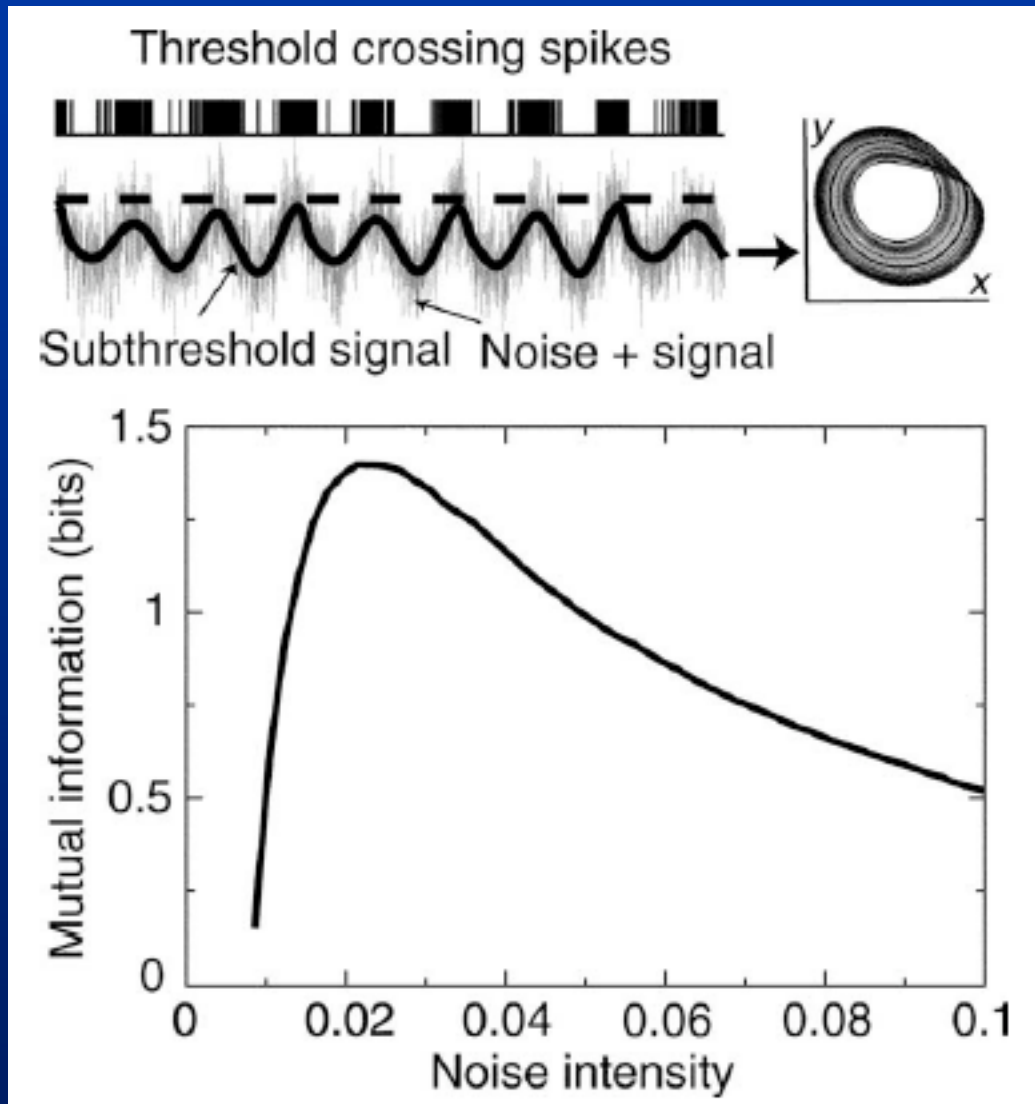
Complexity: young > elderly fallers  
elderly non-fallers > fallers

# Stress Reduces COP Complexity

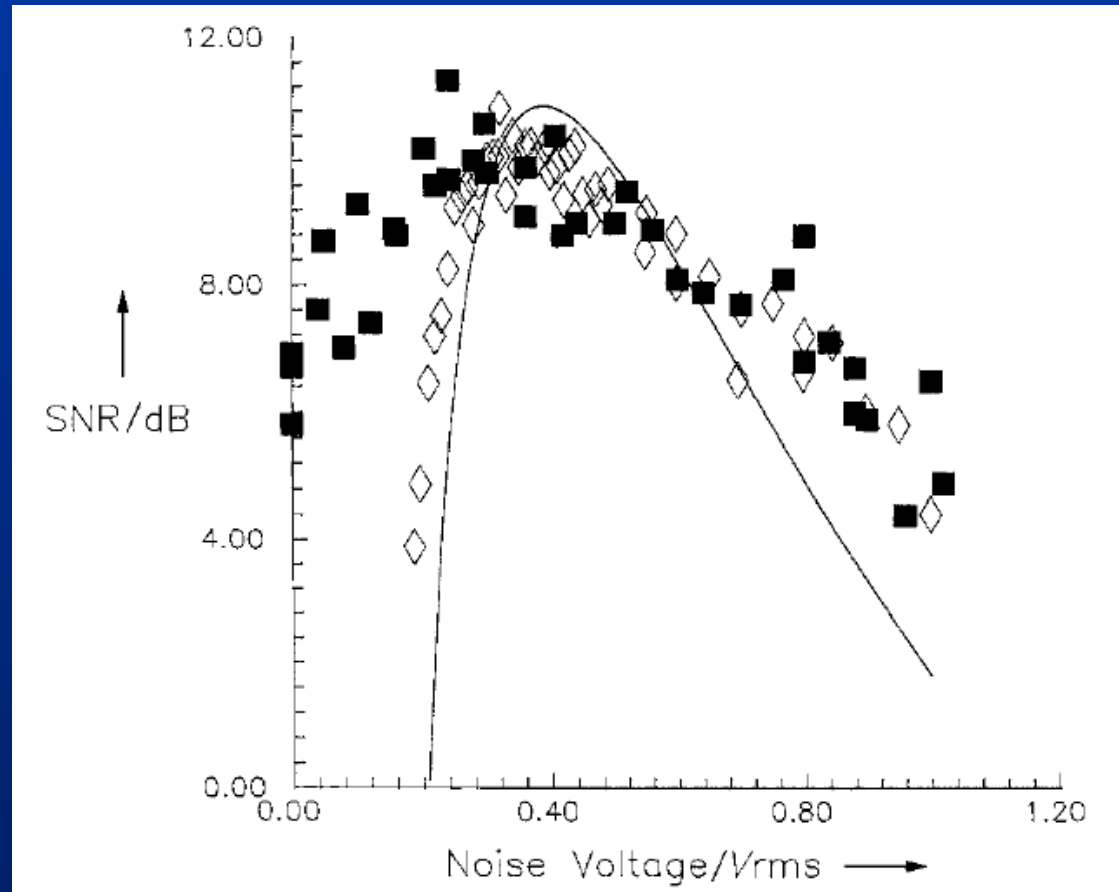


**Kang et al. J Gerontol Med Sci 2009; 64:1304-1311.**

# Stochastic Resonance



# SR: crayfish vs. model



Douglas *et al.* Nature 1993; 365:337

# Stochastic Resonance

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$\sigma = 10$



$\sigma = 90$



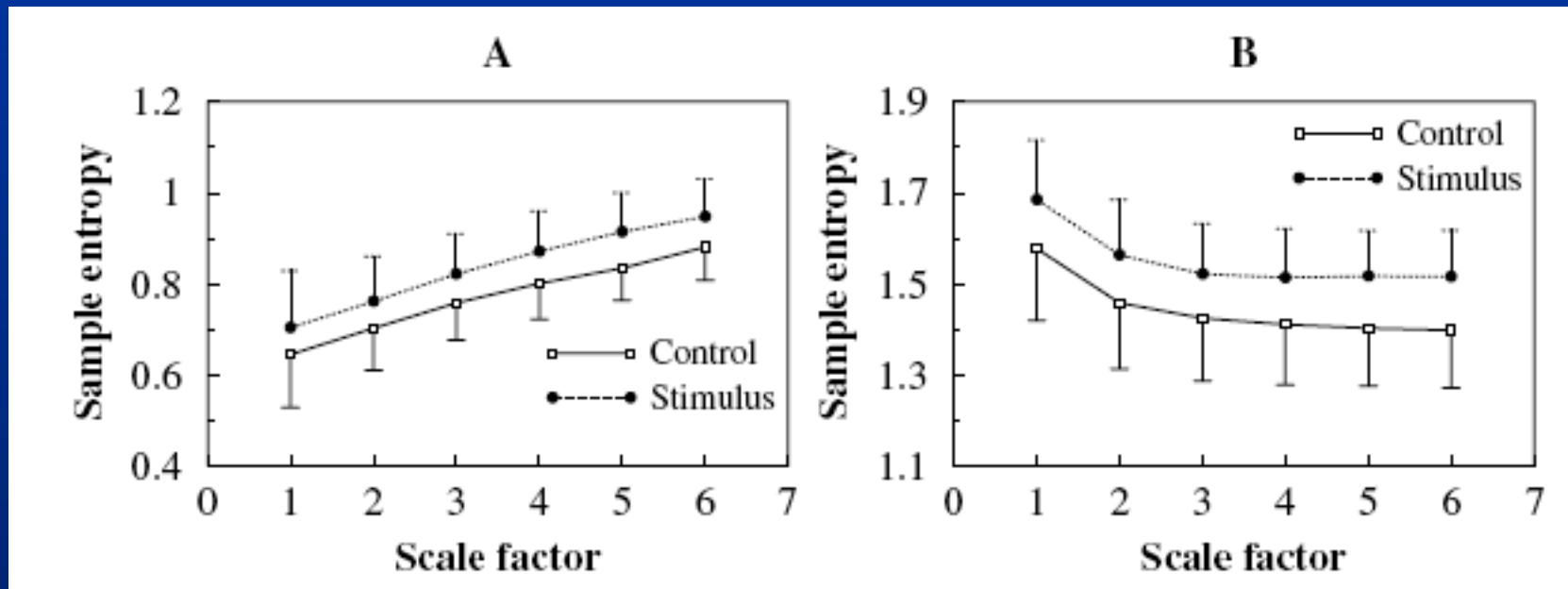
$\sigma = 300$

Simonotto *et al.* Phys Rev Lett 1997; 78:1186



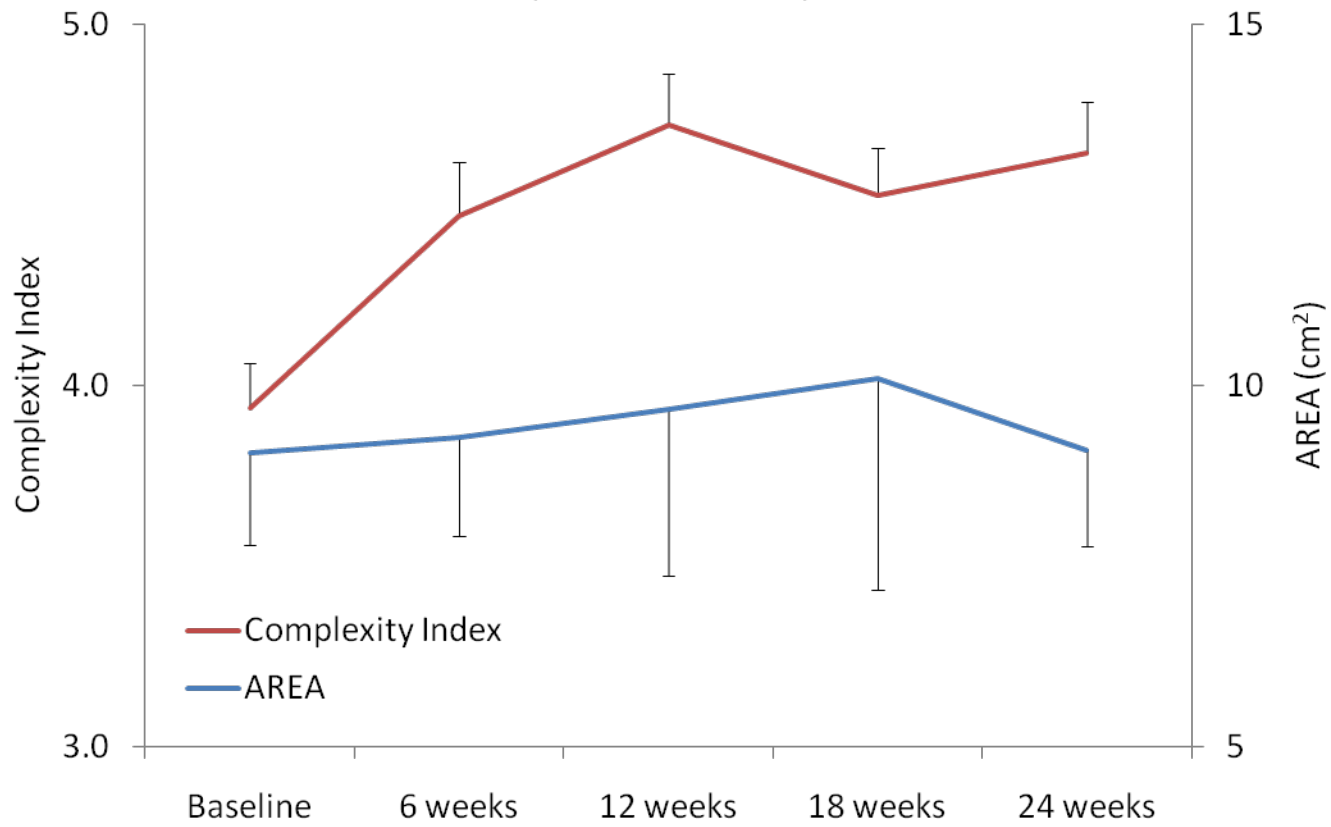
# Sub-threshold Noise Increases Complexity of Sway Dynamics in Elderly (n=12)

One elderly subject (10 trials)



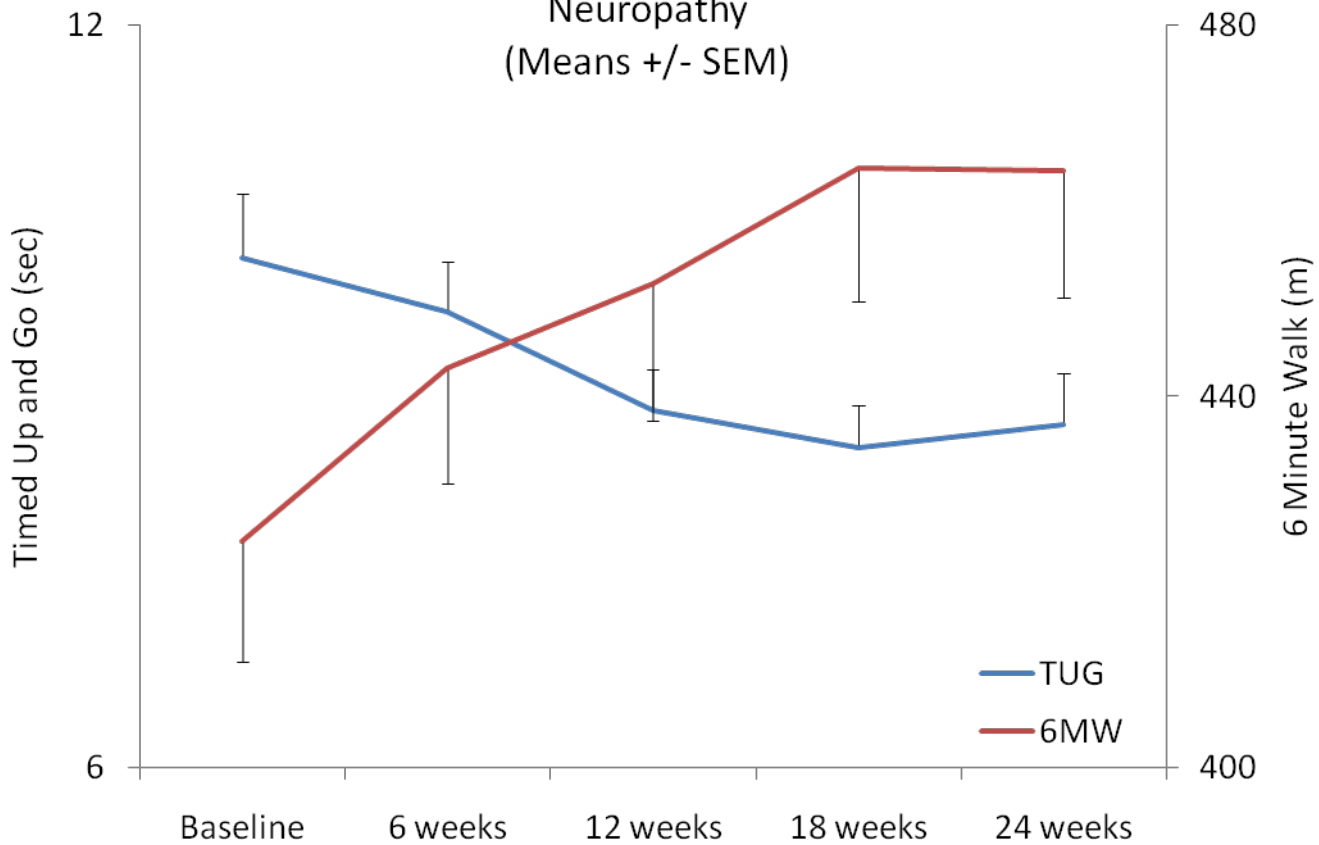
Complexity: input noise > control time series

### Impact of Tai Chi on Postural Sway in Peripheral Neuropathy (Means +/- SEM)



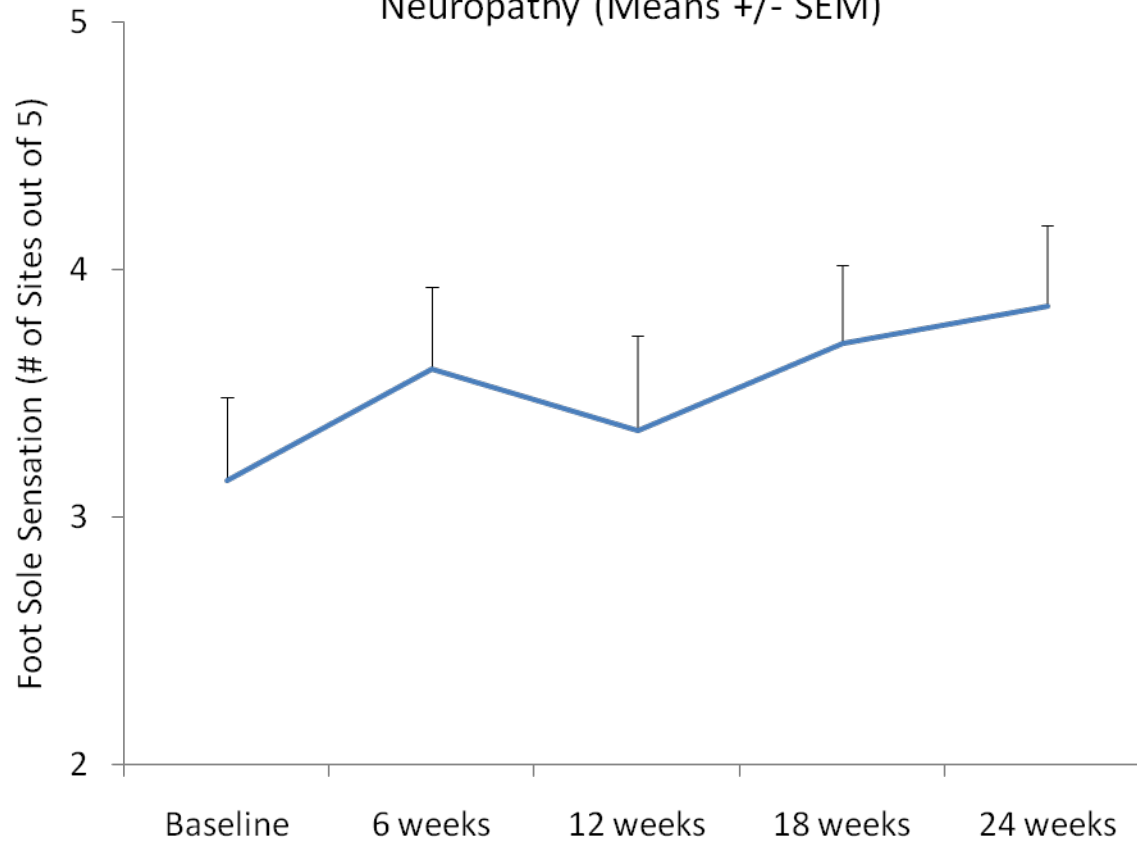
Dr. Brad Manor & Dr. Li Li @ LSU

### Impact of Tai Chi on Physical Function in Peripheral Neuropathy (Means +/- SEM)

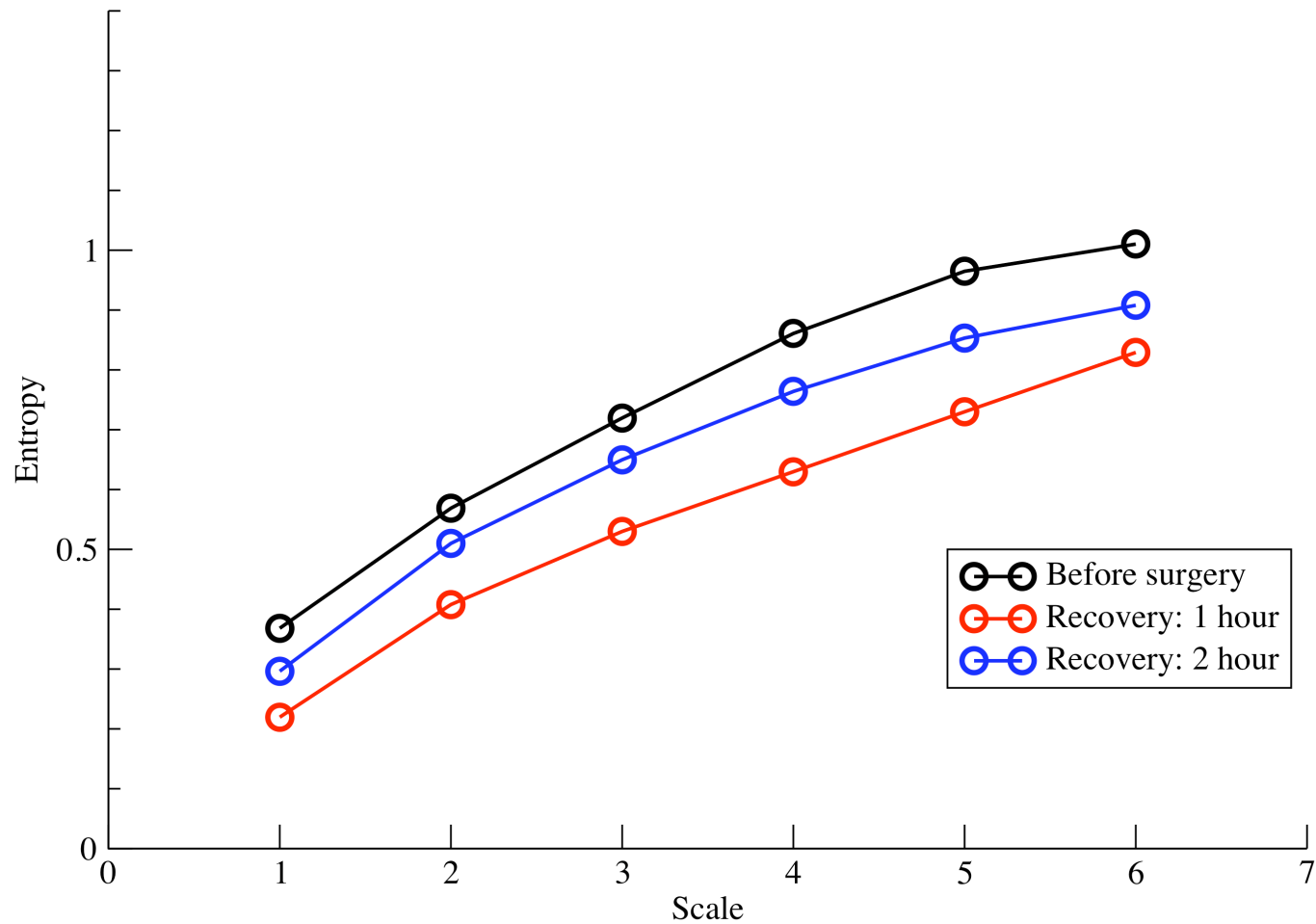


\*\*Completing the timed up and go faster is better, and walking further in the 6 minute walk is better

Impact of Tai Chi on Foot Sole Sensation in Peripheral Neuropathy (Means +/- SEM)



MSE analysis of postural sway time series  
58-year-old female subject



MSE analysis of postural sway time series  
45-year-old male subject

